

# Algorithmic Robotics and Motion Planning

## Introduction

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Fall 2019-2020

Dolce & Gabbana 2018 handbag collection

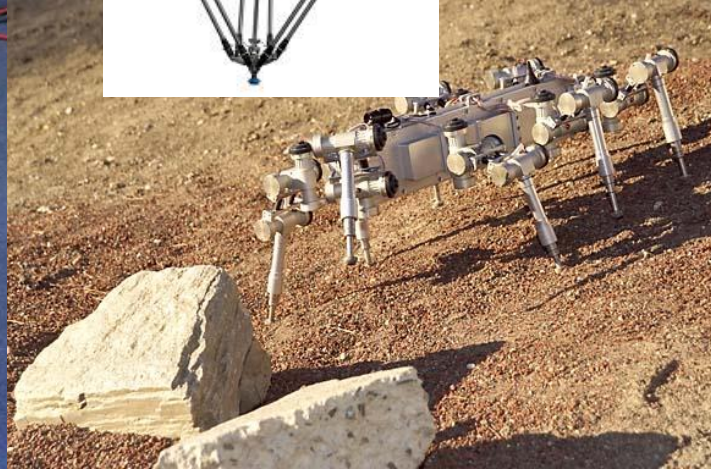
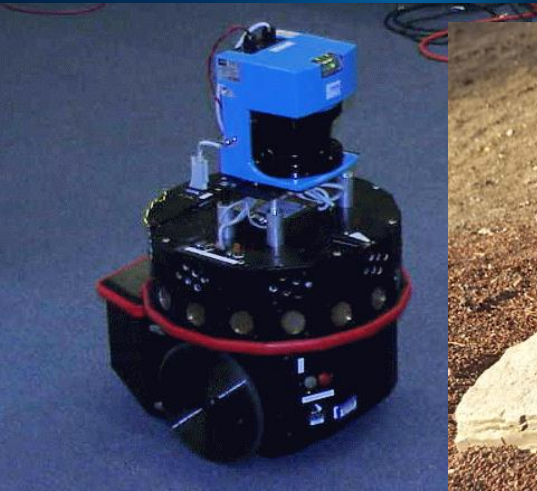
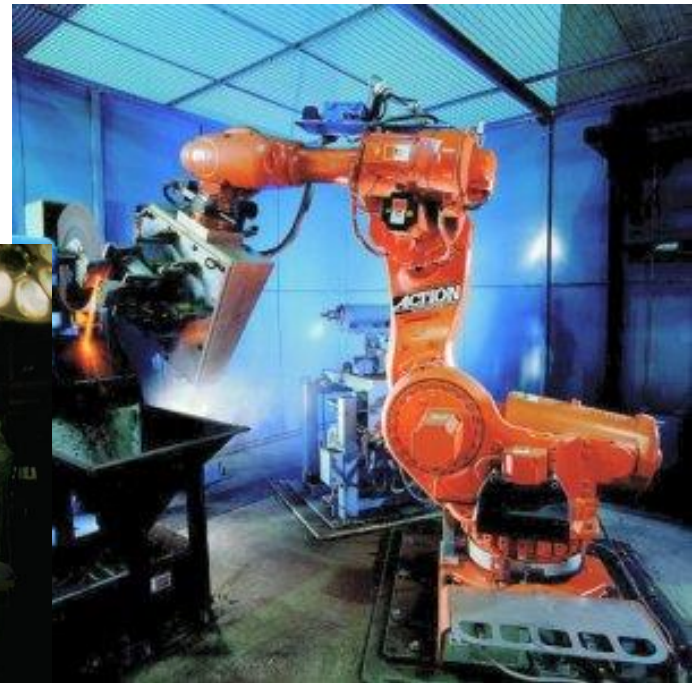
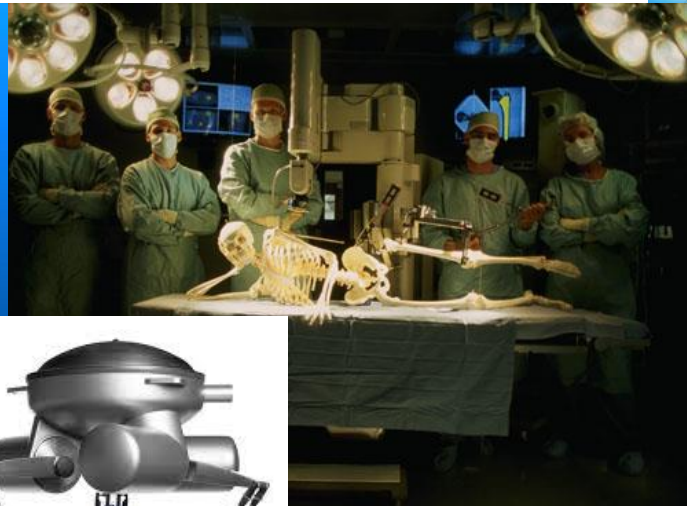
# Today's lesson

- basic terminology
- fundamental problems
- robotics vs. automation
- review of the major course topics
- course mechanics

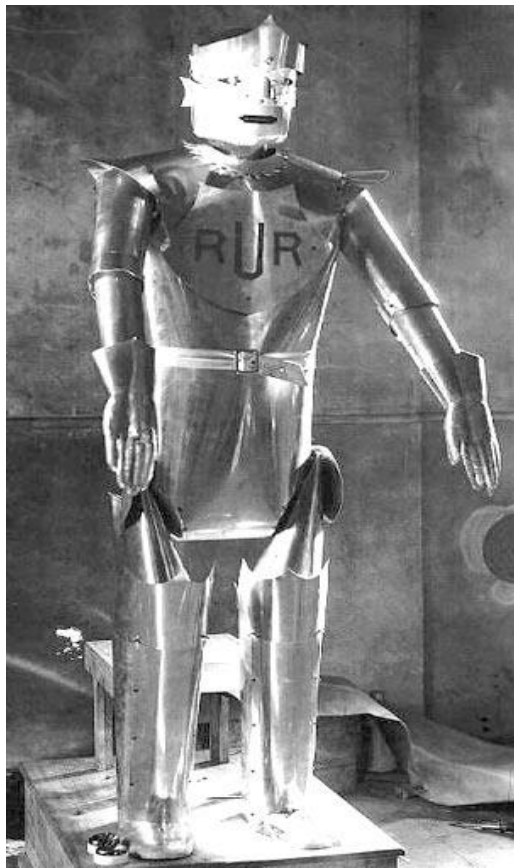
As time permits:

- the Roomba in the café, combinatorics and algorithms

# Robots, take I

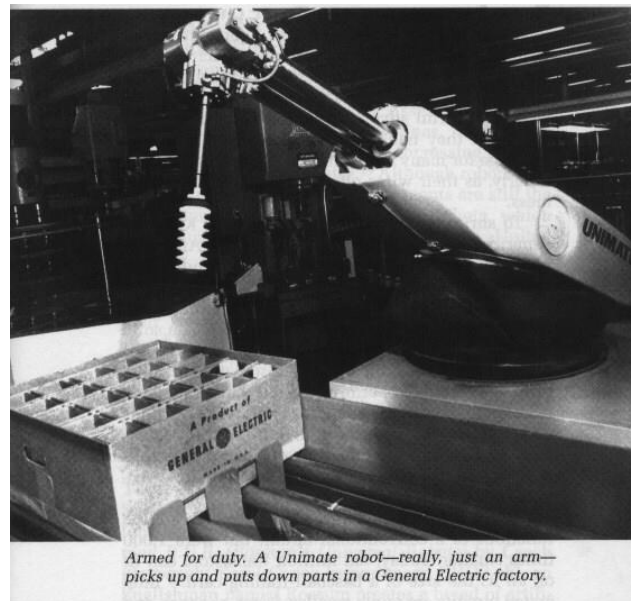


# An extremely brief history of robotics



The RUR robot which appeared in an adaption of Czech author Karel Capek's *Rossum's Universal Robots*. Circa 1930's.

NASA's Curiosity, 2011 →



Armed for duty. A Unimate robot—really, just an arm—picks up and puts down parts in a General Electric factory.

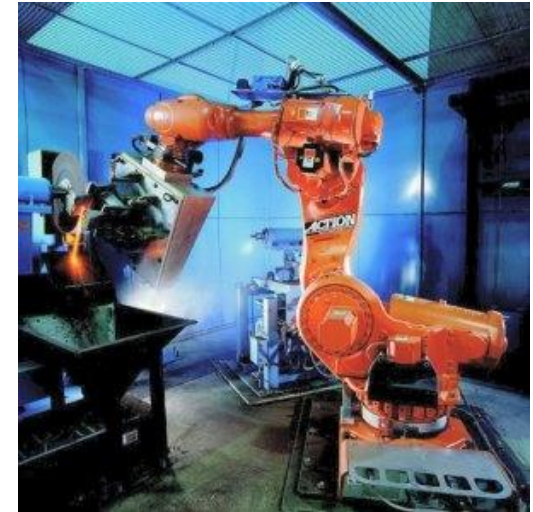
UNIMATE becomes the first industrial robot in use. It was used at the General Motors factory in New Jersey. 1961.



Honda's ASIMO, 2002



# Robotics and robots



[<https://robots.ieee.org/learn/>]

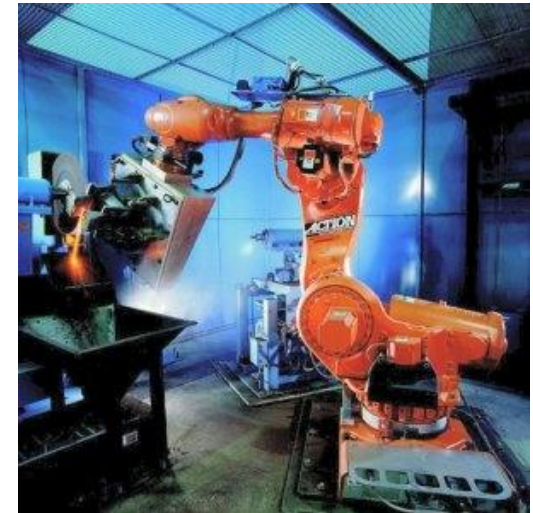
What is a robot?

*A robot is an autonomous machine capable of sensing its environment, carrying out computations to make decisions, and performing actions in the real world.*

!?



# Robotics and robots



Here it will be interesting if

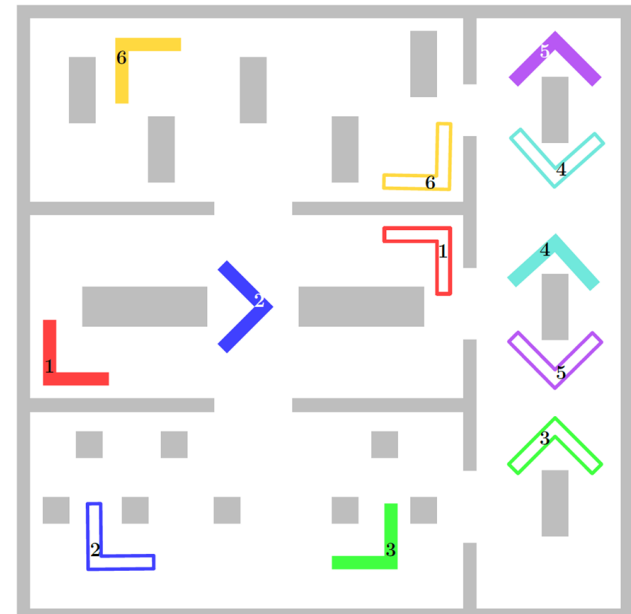
- it is autonomous (at least in part), and
- it has non-trivial motion and/or manipulation capabilities

!?



# Motion planning: the basic problem

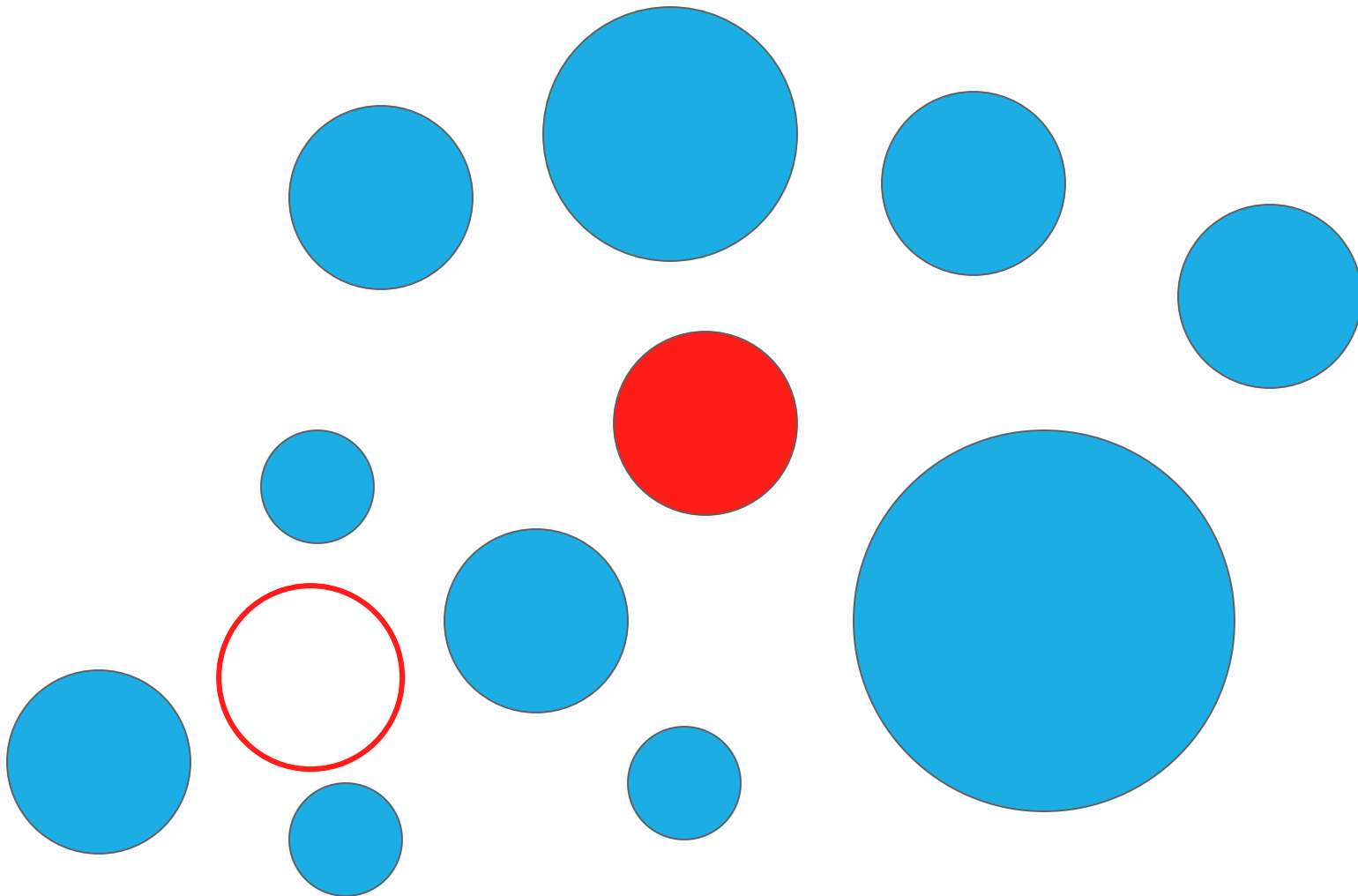
Let  $B$  be a system (the robot) with  $k$  degrees of freedom moving in a known environment cluttered with obstacles. Given free start and goal placements for  $B$  decide whether there is a collision free motion for  $B$  from start to goal and if so plan such a motion.





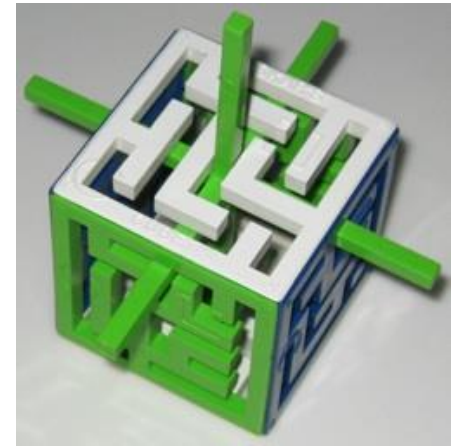
# Example I: The Roomba in the café

A disc moving among discs

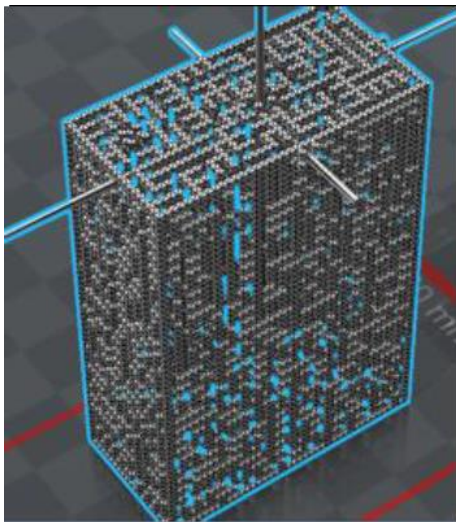


# Example II: Oskar's cube

- MP with 3 translational dofs
- Hint: Scientific American, Sep 1988 issue
- [Jay's Oskar's cubes](#)



[\[oskarvandeventer.nl\]](http://oskarvandeventer.nl)

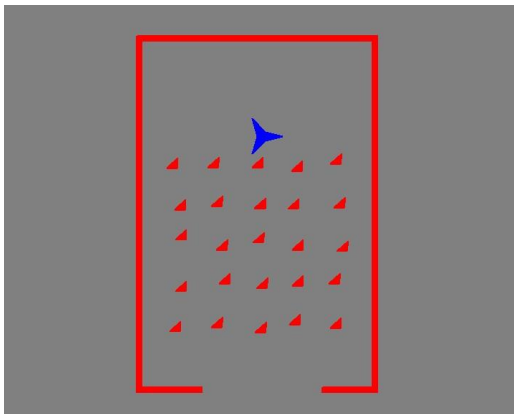
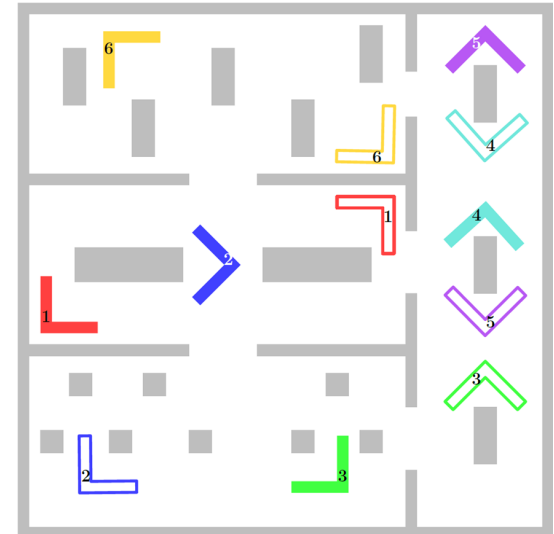


# Terminology

- Workspace
- Configuration space (state space)
- Degrees of freedom (**dofs**)

# Degrees of freedom

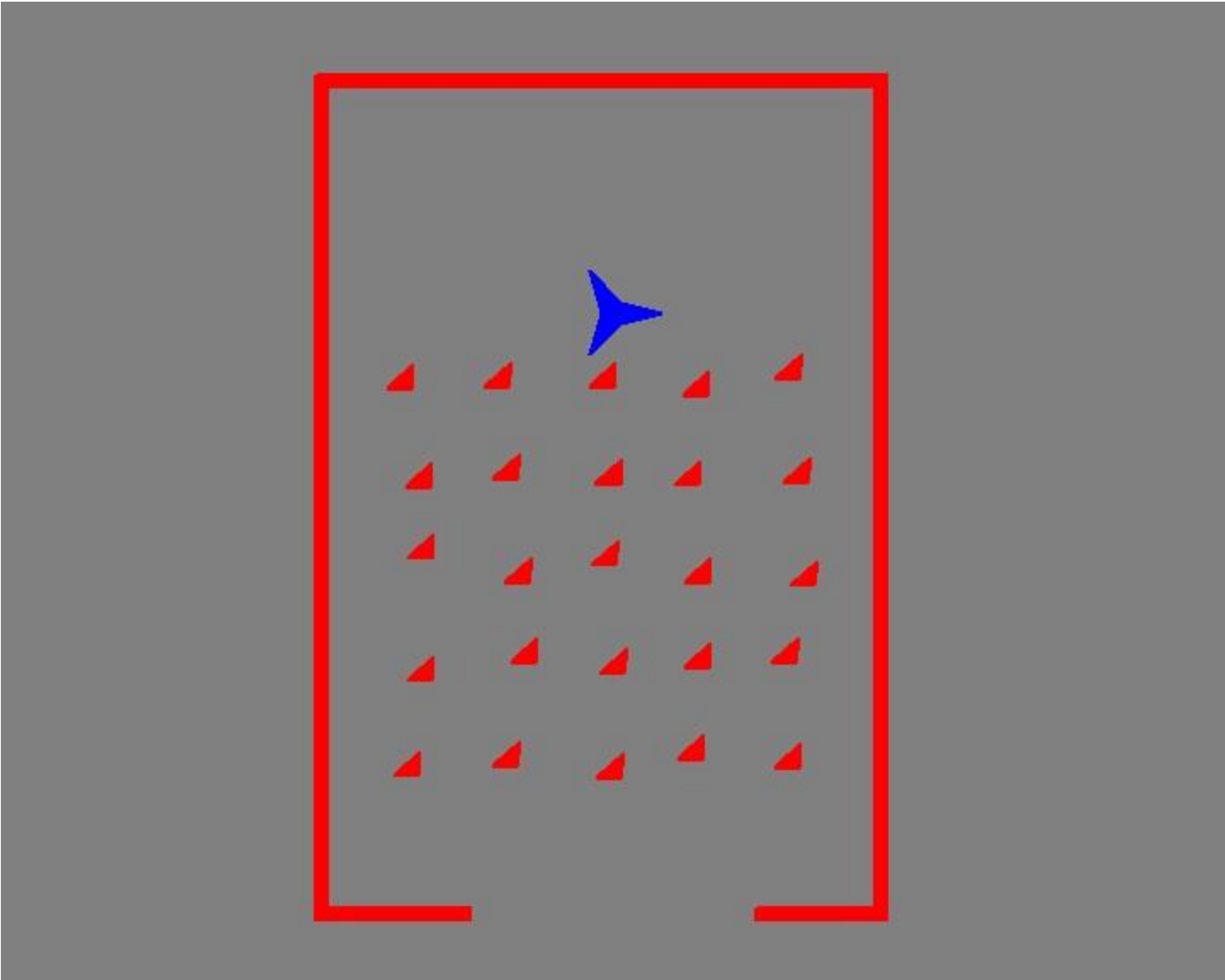
- a polygon robot translating in the plane
- a polygon robot translating and rotating
- a spatial robot translating and rotating
- industrial robot arms
- many robots

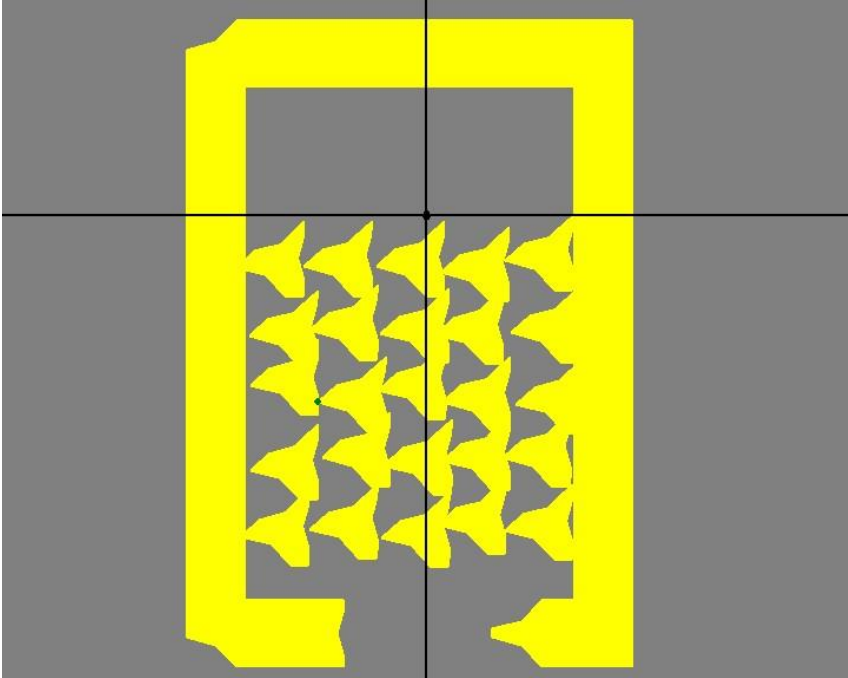
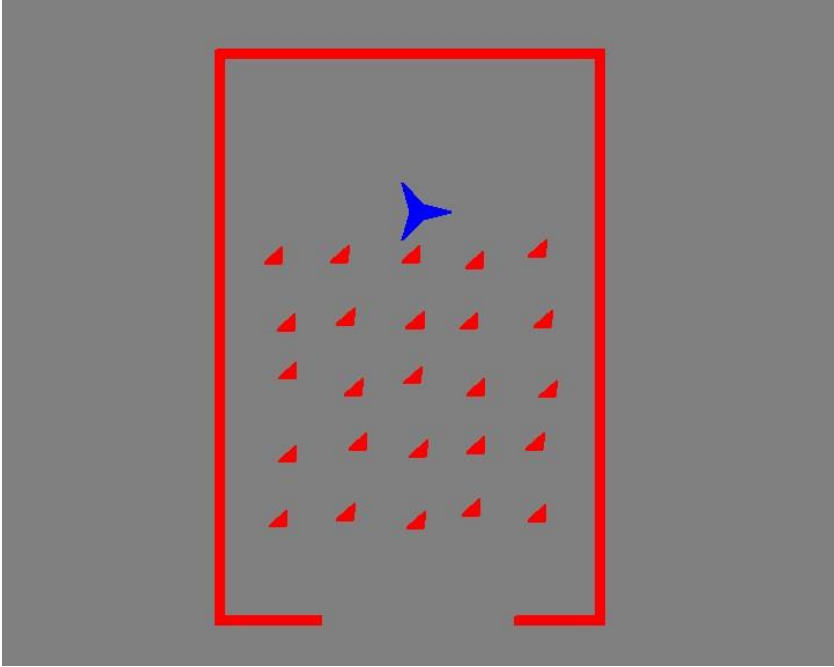


# Configuration space

of a robot system with  $k$  degrees of freedom

- C-space, for short
- also known as state space
- the space of parametric representation of all possible robot configurations
- C-obstacles: the expanded obstacles
- the robot  $\rightarrow$  a point
- $k$ -dimensional space
- point in configuration space: free, forbidden (, semi-free)
- path  $\rightarrow$  curve



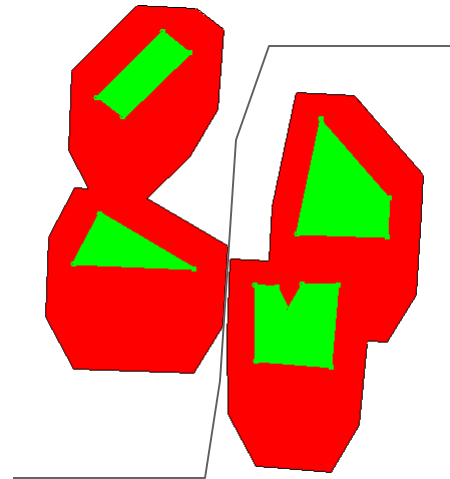
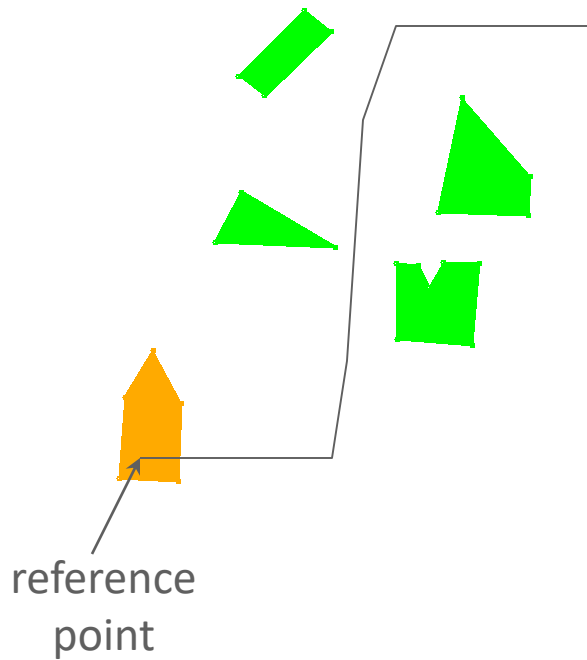


MOVE

# C-obstacles

Q - a polygonal object that moves by translation

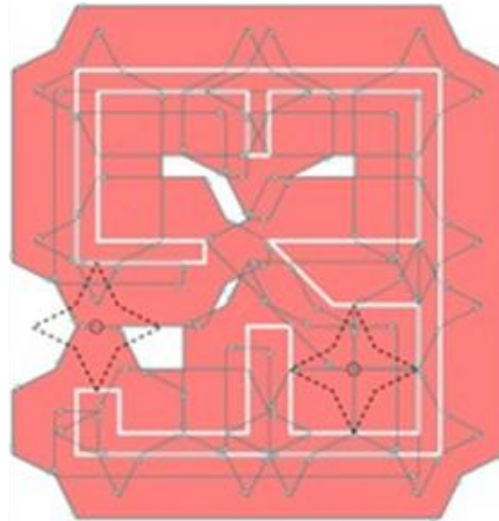
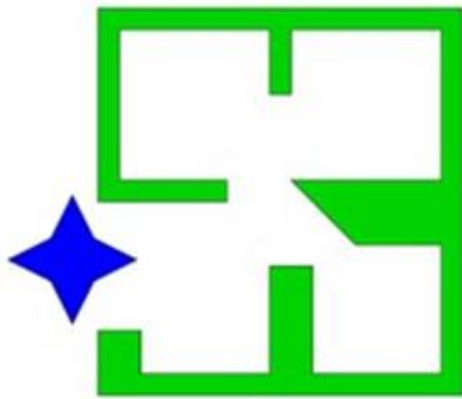
P - a set of polygonal obstacles





# Minkowski sums and translational C-obstacles

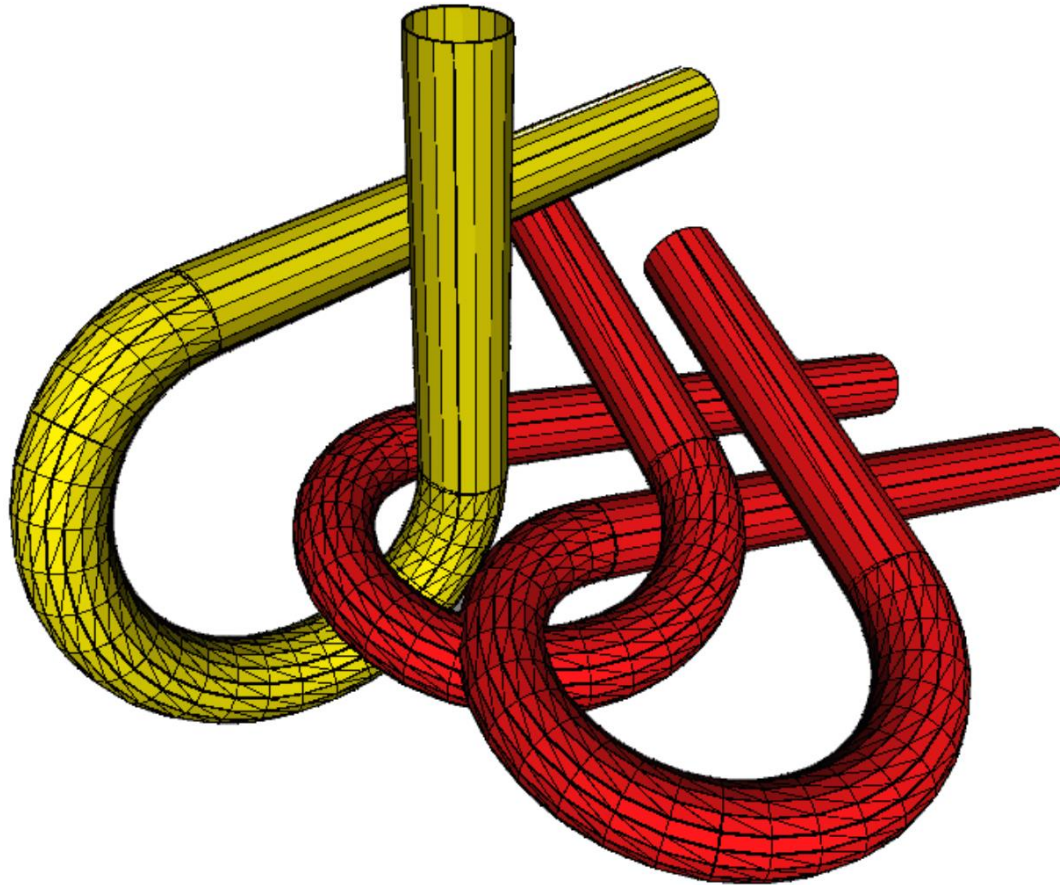
a central tool in geometric computing applicable to motion  
planning and other domains



# More complex systems

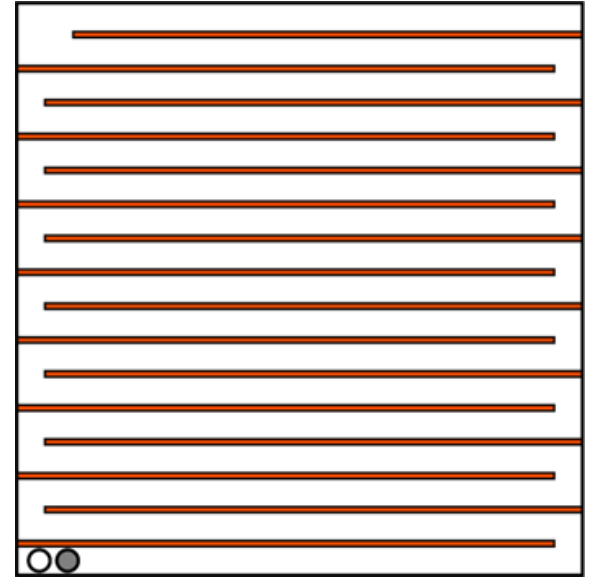
new designs, multi-robot systems, and other moving artifacts  
have many more dofs

# Example III: the $\alpha$ puzzle



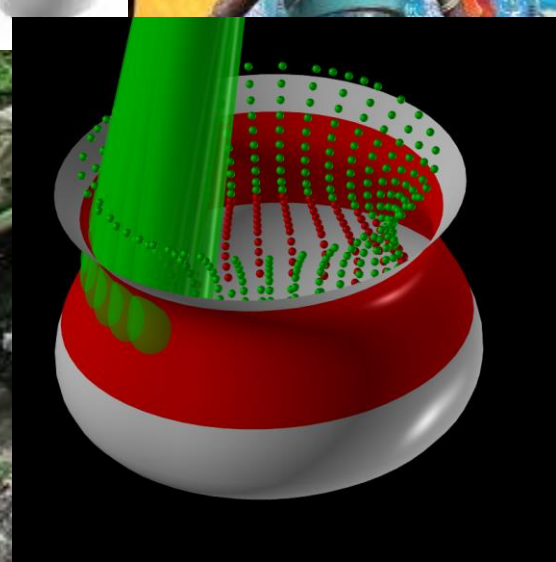
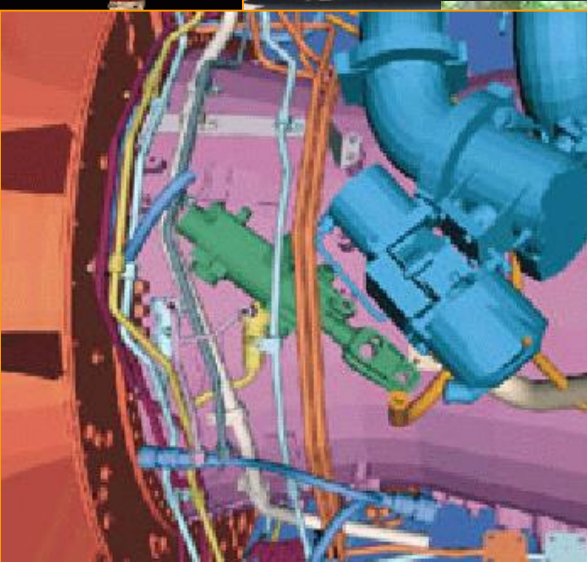
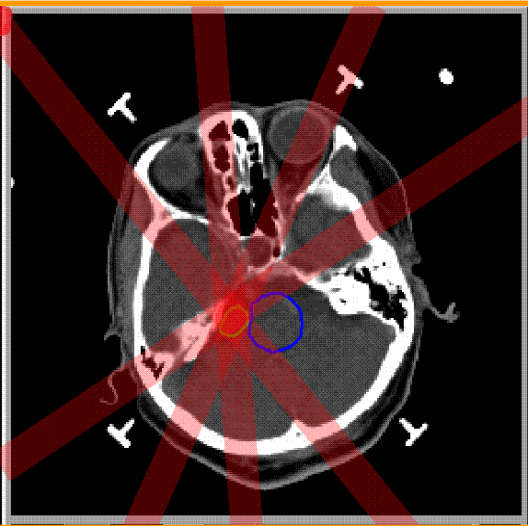
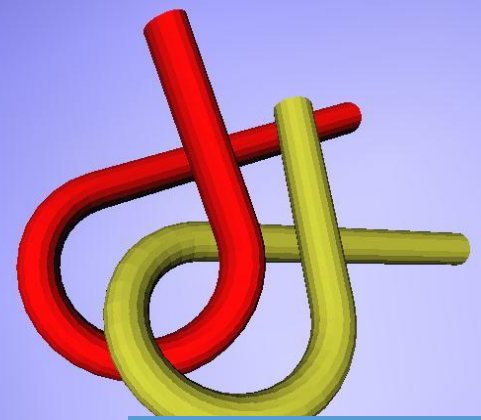
# Types of solutions

- exact
- probabilistic
- hybrid
- heuristic



- major components in practical solutions: **nearest-neighbor search**, **collision detection**

# Robots, take II



# Beyond the basic MP problem

- moving obstacles
- multiple robots
- movable objects
- uncertainty
- nonholonomic constraints
- dynamic constraints
- ...

# Multiple robots

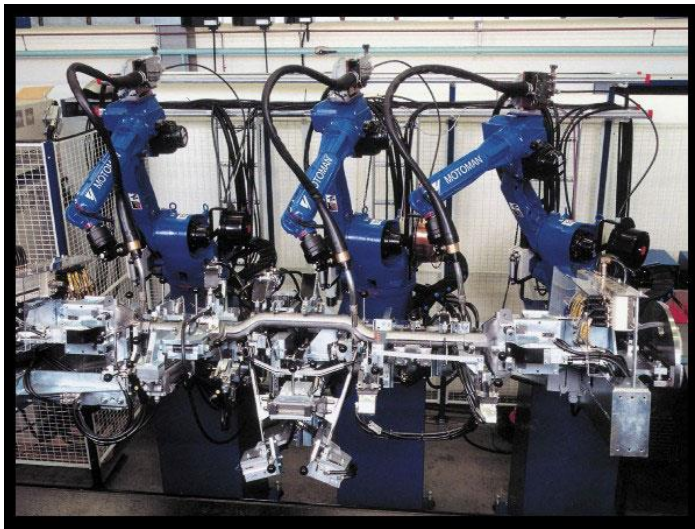
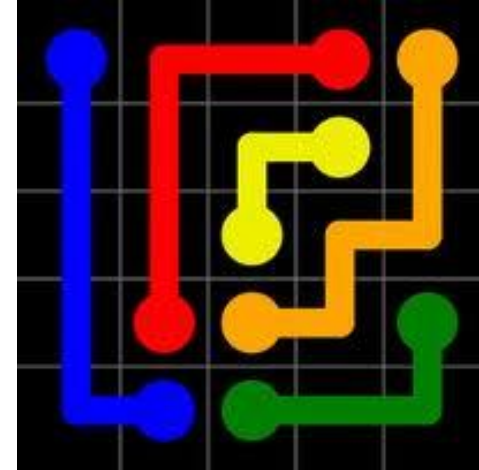
[[home.ustc.edu.cn/~hxiangli](http://home.ustc.edu.cn/~hxiangli)]



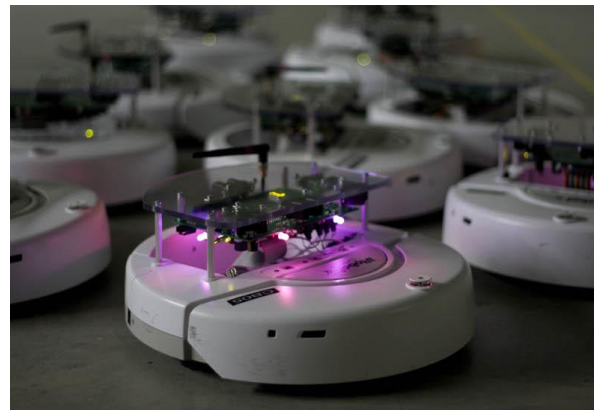
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[flow free]



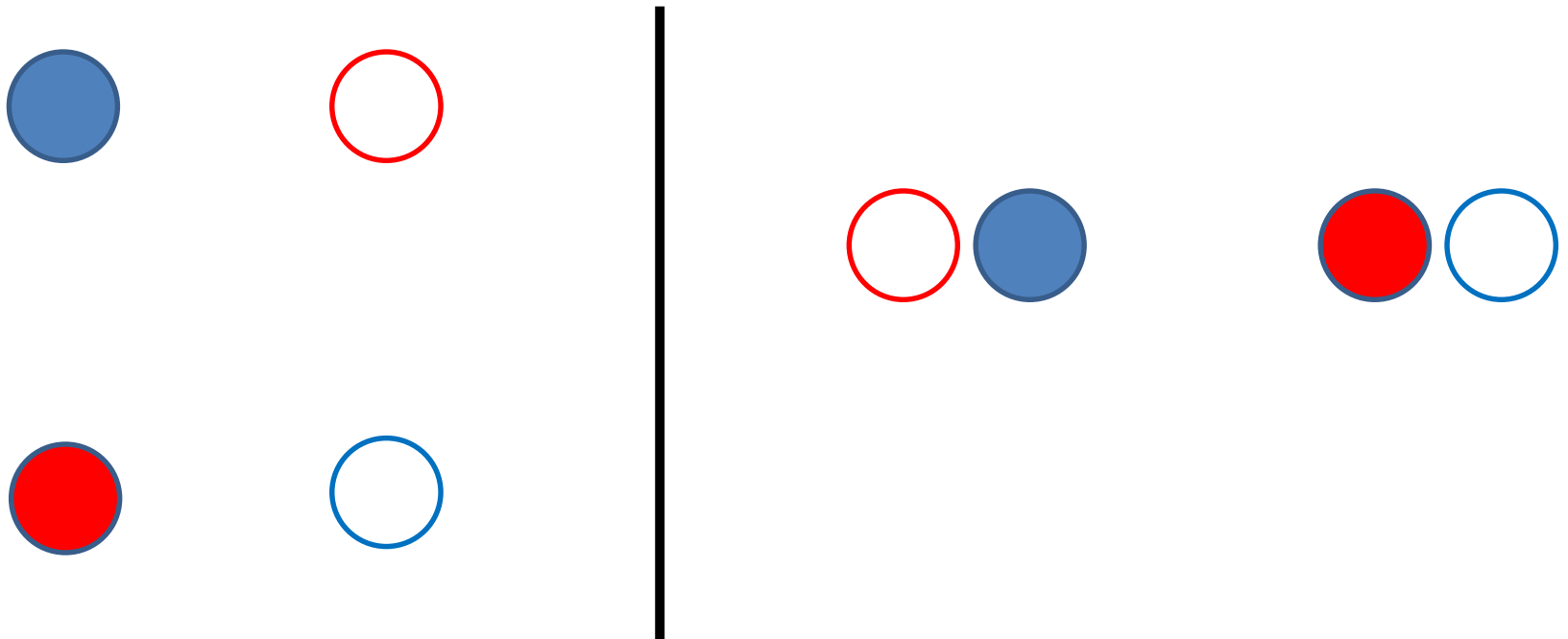
[[autonomy.cs.sfu.ca](http://autonomy.cs.sfu.ca)]



[[lccRobotics.com](http://lccRobotics.com)]

# Problem

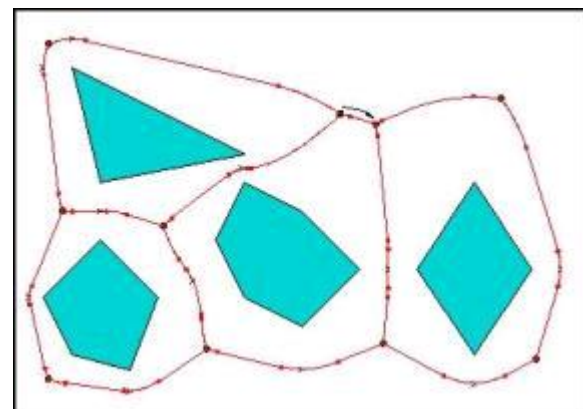
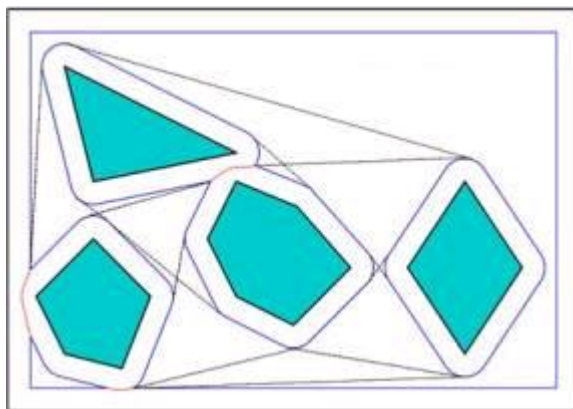
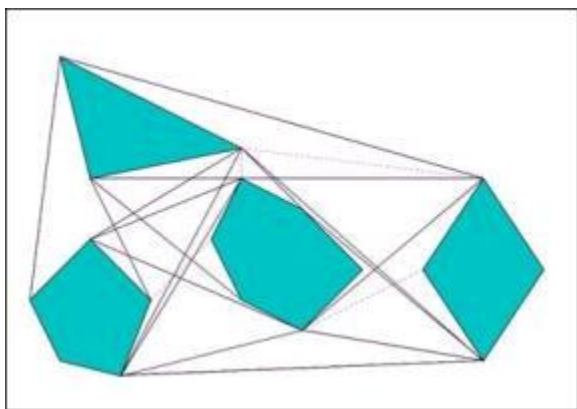
Given two Roomba's, each has to move from given start to goal positions, no obstacles. What are the joint shortest paths (minimum total length)?





# Path quality

- length
- clearance
- combined measures
- minimum energy
- Minimum time
- ...
- hard even in simple settings



## IMPROVING THE QUALITY OF NON-HOLONOMIC MOTION BY HYBRIDIZING C-PRM PATHS

ITAMAR BERGER | BOSMAT ELДАР | GAL ZOHAR | BARAK RAVEH | DAN HALPERIN  
School of Computer Science, Tel-Aviv University, Tel-Aviv, Israel

### INTRODUCTION

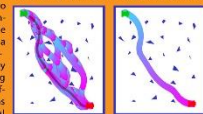
Sampling-based motion planners are an effective means for generating collision-free motion paths. However, the quality of these motion paths, with respect to different quality measures such as path length, clearance, smoothness or energy, is often notoriously low. This problem is accentuated in the case of non-holonomic sampling-based motion planning, in which the space of feasible motion trajectories is restricted. In this study, we combine the C-PRM algorithm by Song and Amato with our recently introduced path-hybridization approach (H-Graphs), for creating high quality non-holonomic motion paths, with combinations of several different quality measures such as path length, smoothness or clearance, as well as the number of reverse car motions.



### H-GRAPHS

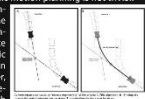
We have recently introduced the path-hybridization approach [2, 3], in which an arbitrary number of input motion paths are hybridized to an output path of superior quality, for a range of path-quality criteria. The approach is based on the observation that the quality of certain sub-paths within each solution may be higher than the quality of the entire path. Specifically, we run an arbitrary motion planner  $k$  times (typically  $k=5-6$ ), resulting in  $k$  intermediate solution paths to the motion planning query. From the union of all the edges and vertices in the intermediate paths we create a single weighted graph, with edge weights set according to the desired quality criterion.

We then try to merge the intermediate paths into a single high-quality path by connecting nodes from different paths with the local planner, and giving the appropriate weights to the new edges. Dijkstra's algorithm is used to find the highest-quality path in the resulting Hybridization-Graph (H-Graph).

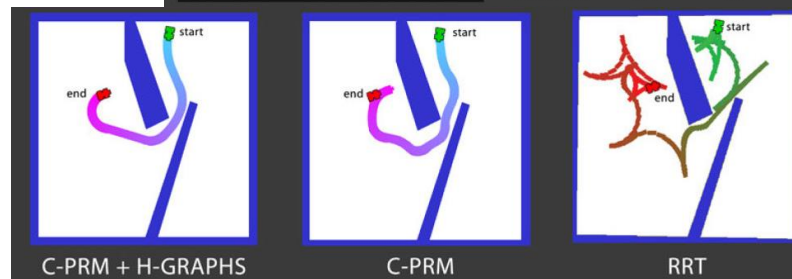


### C-PRM WITH PATH HYBRIDIZATION

While the path hybridization approach has been successfully tested over a range of holonomic motion planning problems with many degrees of freedom, its application to non-holonomic motion planning is not trivial. In particular, whereas it is easy to connect two nearby configurations in the case of holonomic motion, it is in general impossible to linearly interpolate between two states of non-holonomic motion planning, due to the restriction on the set of possible paths. However, we observed that we can simply reverse engineer the original approach taken by C-PRM for car-like motion planning, and go from the approximate roadmap (that is made of arcs and line segments) to the control roadmap (the coarse roadmap that does not include non-holonomic constraints), instead of working the other way around. This allowed us to use the path hybridization approach in a non-holonomic setting, to generate car-like motion paths of high quality.

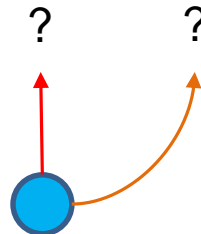


### COMPARISON WITH OTHER METHODS



# Problem

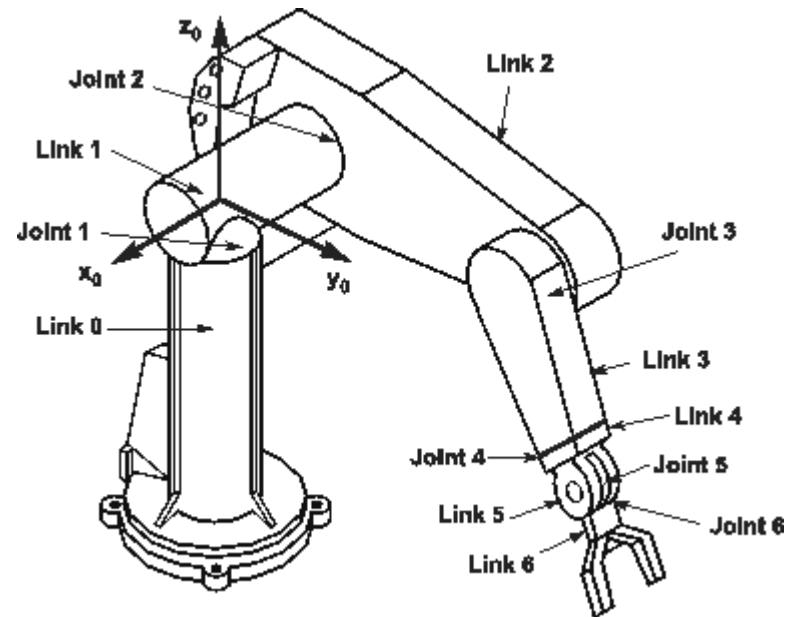
A (point) robot is moving in the plane in the vicinity of a (point) source of nuclear radiation. The cost per unit distance is inversely proportional to the clearance from the source of radiation



typical in robotics:  
multi-objective  
optimization

# Kinematics

- link
- joint
- base
- tcp
- kinematic chain
- direct kinematics
- inverse kinematics



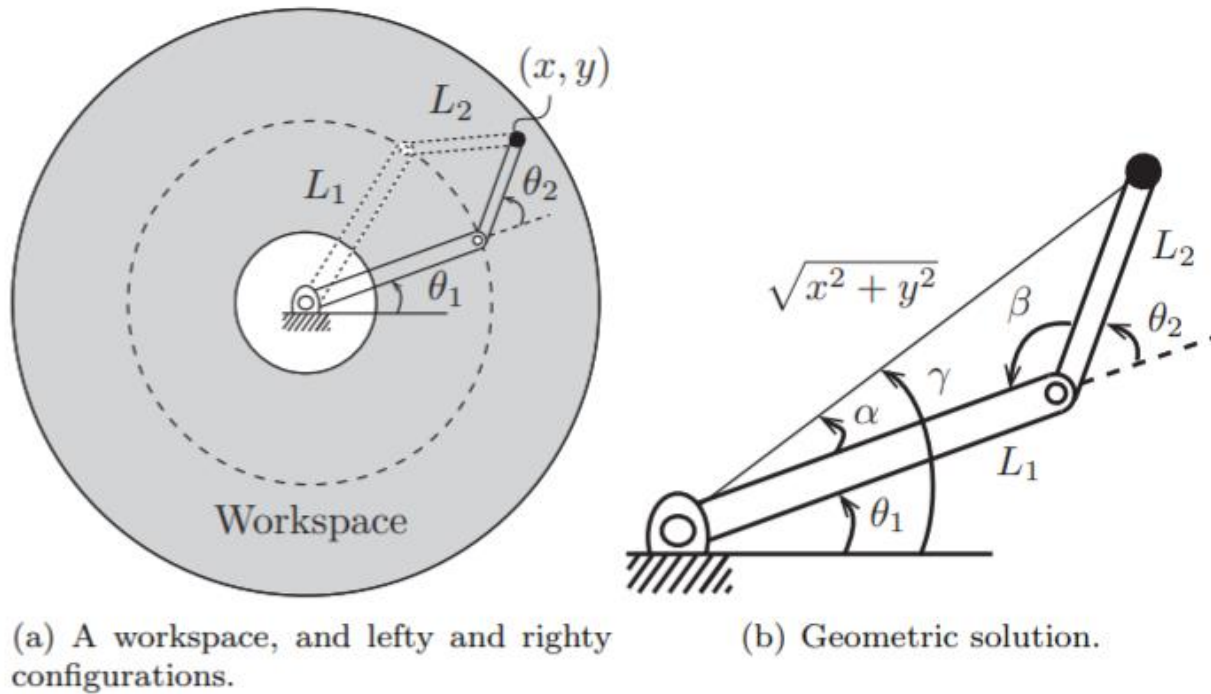
# Inverse kinematics



[Fanuc Iberia]

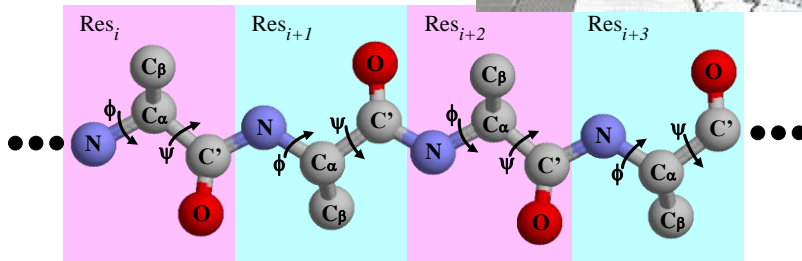
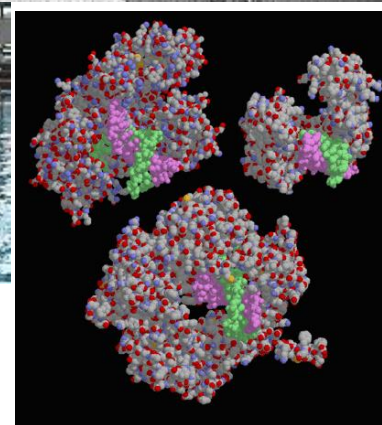
Denavit-Hartenberg 1955, Pieper-Roth 1969

# Inverse kinematics, a simple example



**Figure 6.1:** Inverse kinematics of a 2R planar open chain.

# Large kinematic structures



SWIMMING SNAKE ROBOT

# Algorithmic robotics and automation

typically structured  
predictable environment



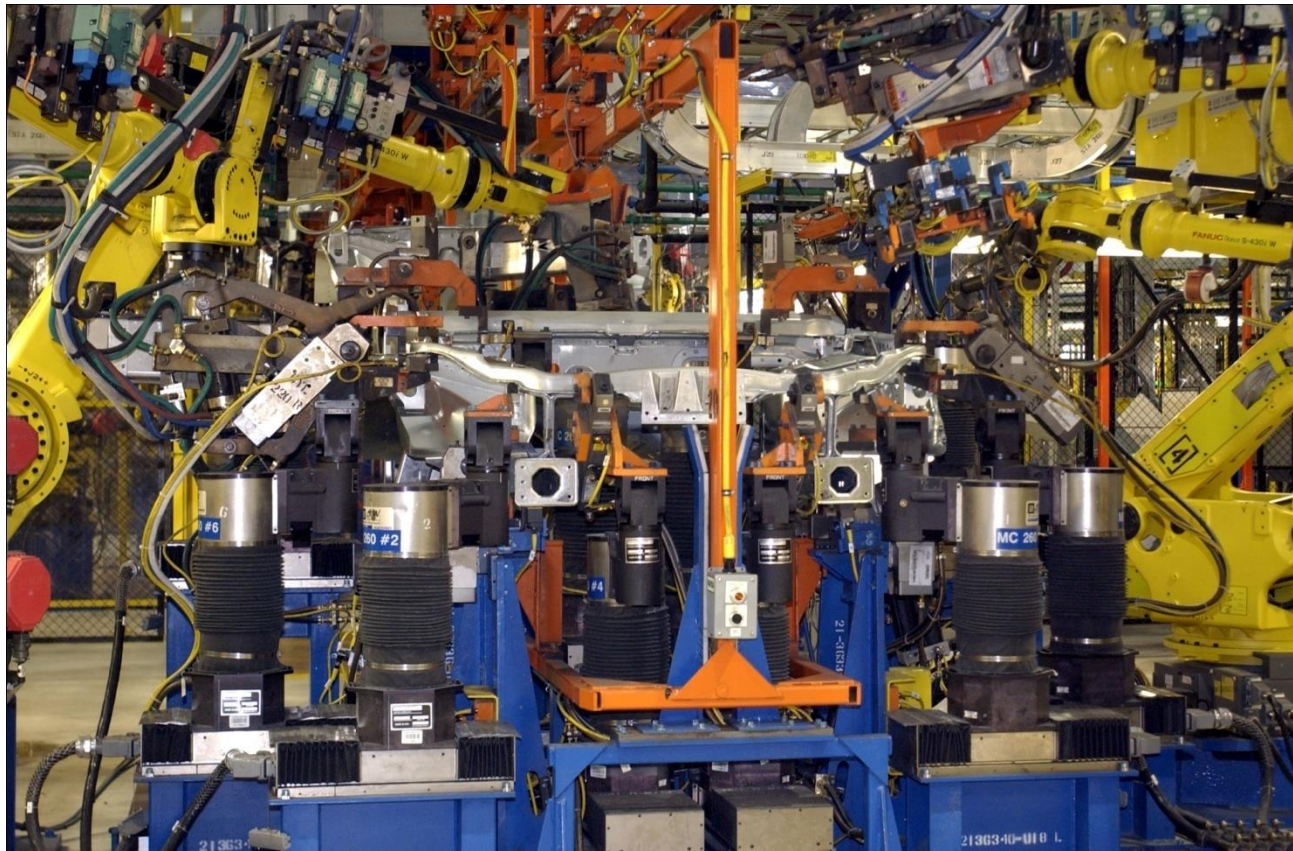
looking toward unpredictable  
environments; lifelong planning

slightly less structured  
environment



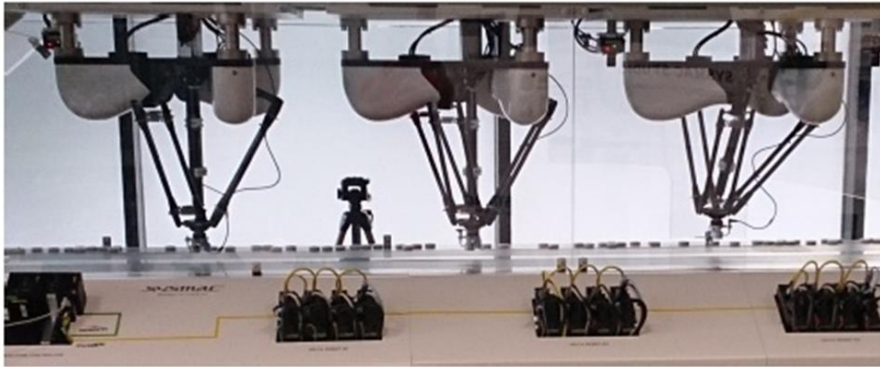
Q: is the cloth always below the line  
through the two fingers?

# Cluttered environments

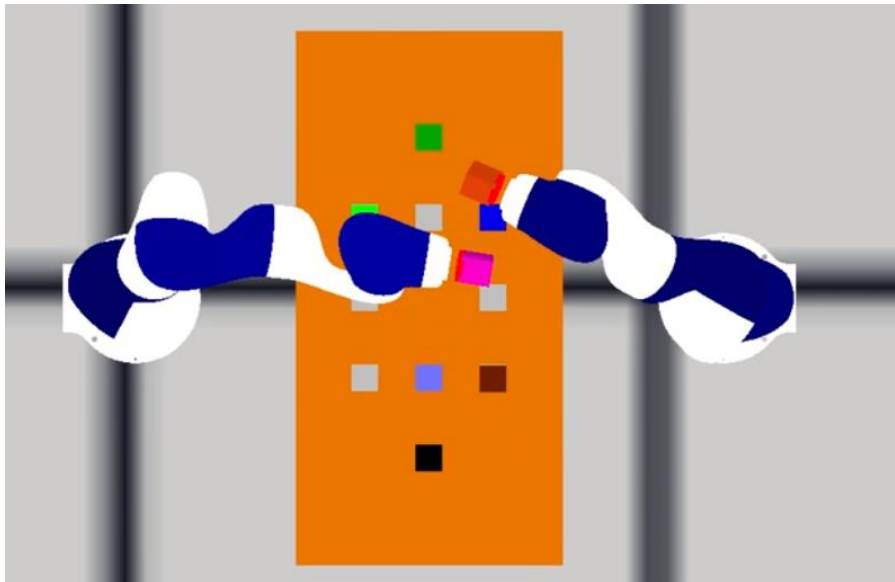




# Algorithmic robotics and automation



Packaging: collision detection in tight settings



Dual arm object rearrangement

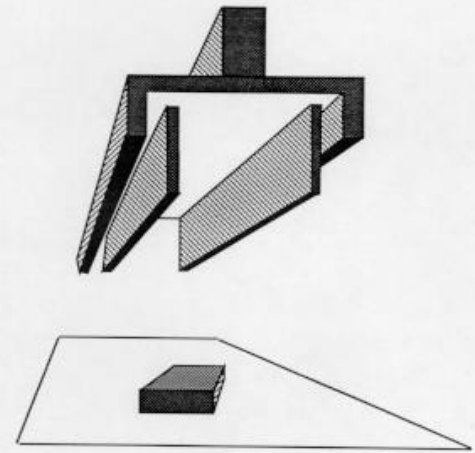
# Algorithmic robotics, sensorless manipulation

Example:

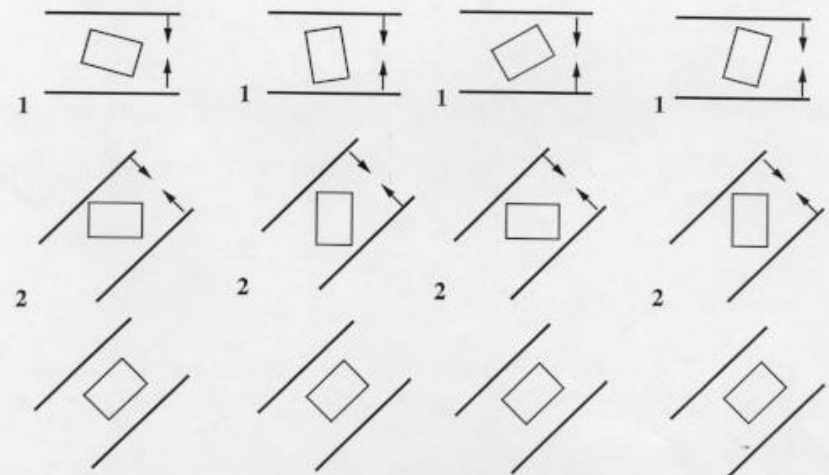
the parallel jaw gripper [Goldberg]

[VIDEO](#)

Hardware:



Software:



# About the course

Setting your expectations

# The course at a glance

## The main themes

### Algorithmic foundations

- Part I: Complete (exact) methods
- Part II: Sampling-based methods
- Part III: Multi-robot motion planning

### Robotics at large

- Students mini-talks
- Guest lectures

# Algorithmic foundations

- Part I: **Complete (exact) methods**
  - Arrangements, Minkowski sums, visibility graphs, Voronoi diagrams, Collins decomposition
- Part II: **Sampling-based methods**
  - Roadmaps, single vs. multi-query structures, probabilistic completeness, asymptotic optimality, collision detection
- Part III: **Multi-robot motion planning**
  - Hardness, labeled vs. unlabeled, separation assumptions, exact algorithms, SB planners

# Guest lectures

- **Guy Hoffmnan**, Cornell, 23.12.19: TED  
Designing Robots and Designing with Robots: New Strategies for an Automated Workplace
- **Ilana Nisky**, BGU, 6.1.20:  
Haptics for the Benefit of Human Health
- **Oren Salzman**, Technion, 30.12.19:  
Asymptotically-Optimal Inspection Planning with Application to Minimally-Invasive Robotic Surgery
- **Aviv Tamar**, Technion, 2.12.19:  
Machine Learning in Robotics
- **Lior Zalmanson**, TAU, 25.11.19:  
Trekking the Uncanny Valley --- Why Robots Should Look Like Robots?

# The course at a glance

Additional topics, as time permits

- SLAM
- ROS
- Robot kinematics
- Large kinematic structures

The course at a glance

## Setting your expectations, I

### Algorithmic foundations

- Part I: Complete (exact) methods
- Part II: Sampling-based methods
- Part III: Multi-robot motion planning

### Robotics at large

- Students mini-talks
- Guest lectures



# Course mechanics

- requirements (% of the final grade):
  - assignments (40%)
  - mini talk (10%)
  - final project (50%)
- assignment types:
  - () theory
  - (p) programming, solo
  - (p2) programming, you can work and submit in pairs
- office hours: by appointment

# Tailor the tasks to your interests (in part)

- 40% fixed: the assignments
- 60% adaptable: mini talk and final project

# Course team

- Instructor: Dan Halperin
- Teaching assistant: Michal Kleinbort
- Grader: Yair Karin
- Software help: Michal Kleinbort, Nir Goren

# Background knowledge

## Setting your expectations, II

- Basic formal prerequisites: Algorithms, Data structures, Software1
- This course vs. Computational Geometry:
  - knowledge of some tools at the “API level”
  - basic reading: CG book by de Berg et al, Chapters 1&2
  - needed material will be discussed in the recitation
- Programming:
  - Python
  - some C++ might be unavoidable—we aim to provide Python bindings to C++ code, where possible
  - support will be provided in the recitation and in office hours

# Main class vs recitation

- Main class, Monday 16-19, **mandatory attendance**
- Recitation, Monday 19-20, optional

topics of recitation: support, computational geometry tools,  
software tools

# Mini talks

- 15 minutes
- or, 30 minutes for two students together
- topic of your choice; requires approval
- references to various up-to-date sources follow
- preferably involving more than one robot
- deadline for selecting a topic: November 25th, 2019

# Final project

- compact
- topic of your choice; requires approval
- algorithm+experiments, but **other options possible**
- various projects will be proposed by the course team
- preferably involving more than one robot
- deadline for selecting a topic: January 5th (Sunday!), 2020



# Course site

<http://acg.cs.tau.ac.il/courses>

**Algorithmic Robotics and Motion Planning, Fall 2019-2020**

includes bibliography, lesson summary, assignments and more



# Conferences and journals

- Conferences
  - [ICRA](#), IROS, RSS, WAFR, ...
- Journals
  - IJRR (International journal of Robotics Research),
  - IEEE TOR (Transactions on Robotics),
  - IEEE RA-L (Robotics and Automation Letters),
  - IEEE TASE (Transactions on Automation Science and Engineering),
  - Autonomous Robots,
  - ...
- New conference on multi-robot systems: MRS

# Bibliography I

## Books

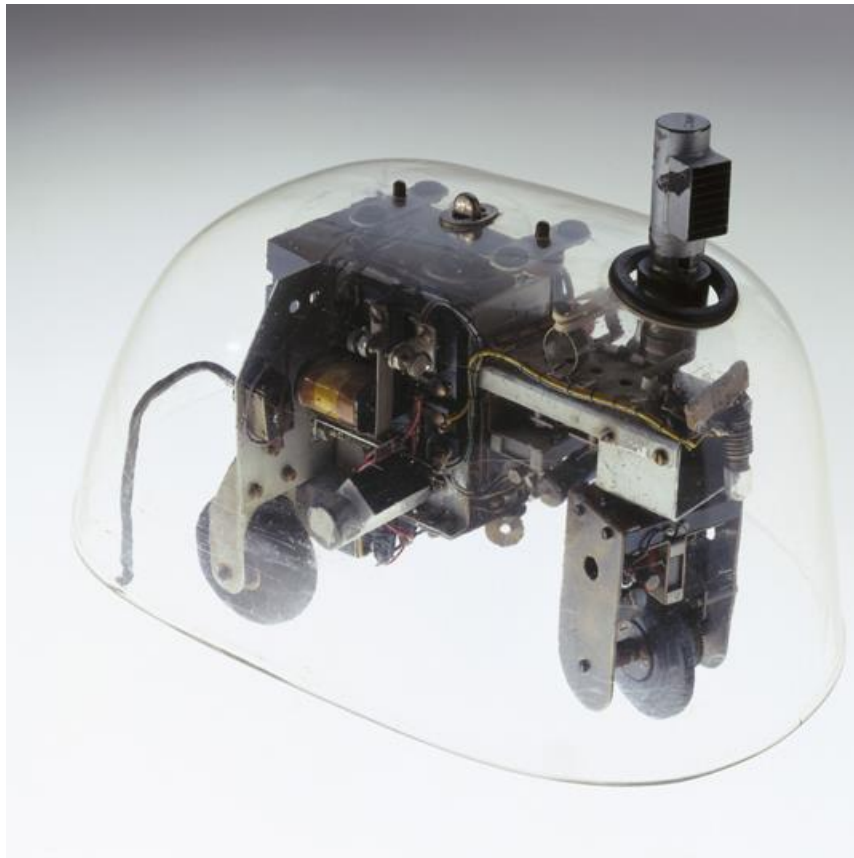
- [Planning Algorithms](#), Steve LaValle, Cambridge University Press, 2006 (free online)
- Robot Motion Planning, Jean-Claude Latombe, Kluwer , 1991, later Springer
- [Modern Robotics](#), Kevin Lynch and Frank Park, Cambridge University Press, 2017 (free online)
- Principles of Robot Motion: Theory, Algorithms, and Implementations, Choset et al, MIT Press, 2005  
in particular Chapter 7
- [Computational Geometry: Algorithms and Applications](#), de Berg et al, 3rd Edition, Springer, 2008

# Bibliography II

## Surveys

- [Sampling-Based Robot Motion Planning](#), Oren Salzman, Communications of the ACM, October 2019
- [Sampling-Based Robot Motion Planning: A Review](#), Elbanhawi and Simic, IEEE Access, 2014 (free online)
- [Robotics](#), Halperin, Kavraki, Solovey, in Handbook of Computational Geometry, 3rd Edition, 2018
- [Algorithmic Motion Planning](#), Halperin, Salzman, Sharir, Handbook of Computational Geometry, 3rd Edition, 2018

# Before the end, a little more history



- Grey Walter's tortoises  
~1948
- Turing's visit to the Science  
Museum 1951

THE END